

ECFA

LEVEL-1

MOS TRANSISTOR MODEL

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References

- **B. Razavi, "Design of Analog CMOS Integrated Circuits", Mc Graw-Hill, 2001.**
- **K. Martin & D. Johns, "Analog Integrated Circuits Design", John Wiley, 1997.**
- **W. Sansen & K. Laker, "Design of Analog Integrated Circuits & Systems", Mc Graw-Hill, 1994.**
- **P. Gray & R. Meyer, "Analysis and Design of Analog Integrated Circuits", third edition, John Wiley 1993.**
- **G. Temes & R. Gregorian, "Analog MOS Integrated Circuits for Signal Processing", John Wiley, 1986.**
- **Jacky Porte, "OCEANE: Outils pour la Conception et l'Enseignement des circuits intégrés ANalogiquEs", <http://www-asim.lip6.fr/recherche/analog/oceane/>**

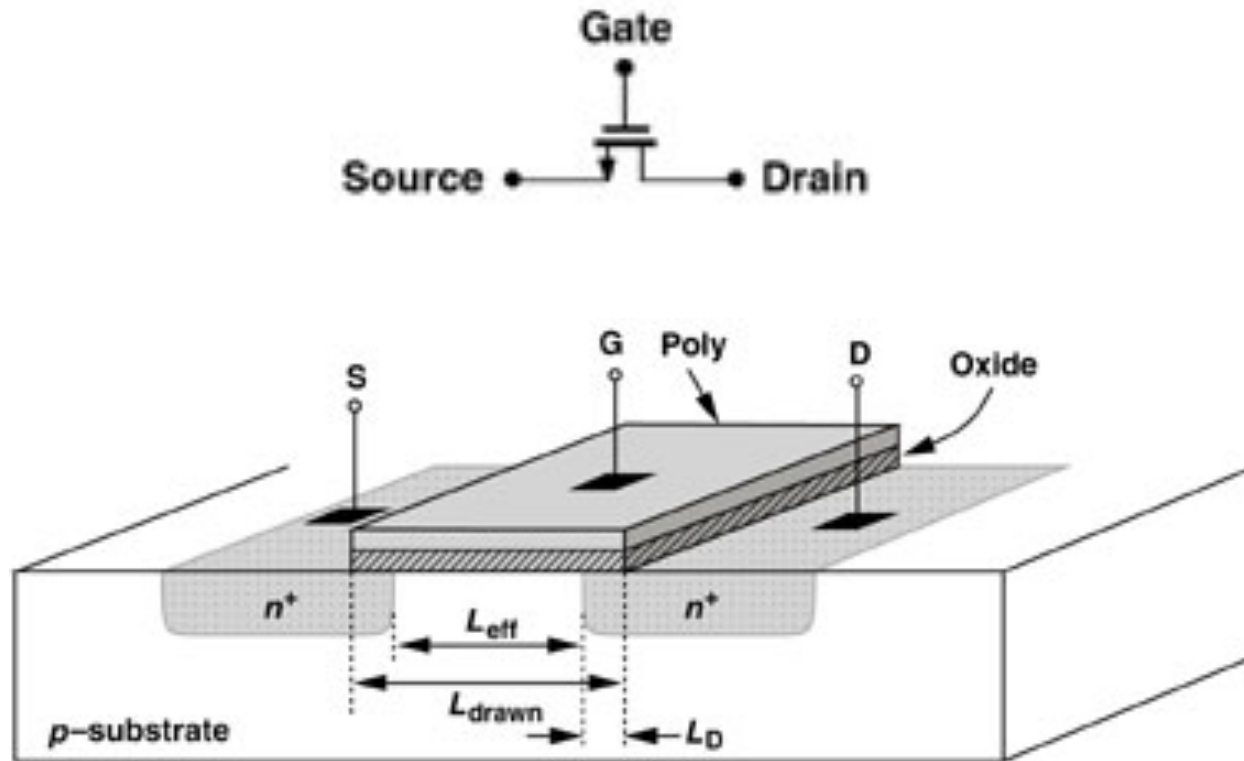
Lecture I

Basic MOS Device Physics

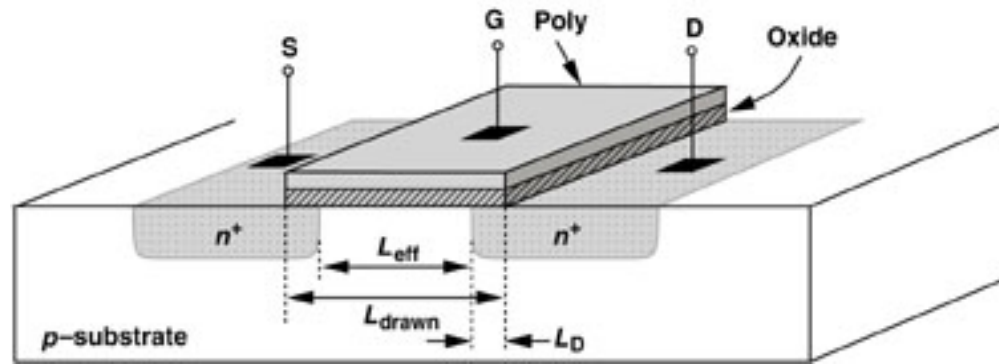
Basic MOS Device Physics

- **The MOSFET structure**
- **MOS I/V Characteristics**
- **Second Order Effects**
- **MOS Device models**

MOS Device Structure



NMOS Structure

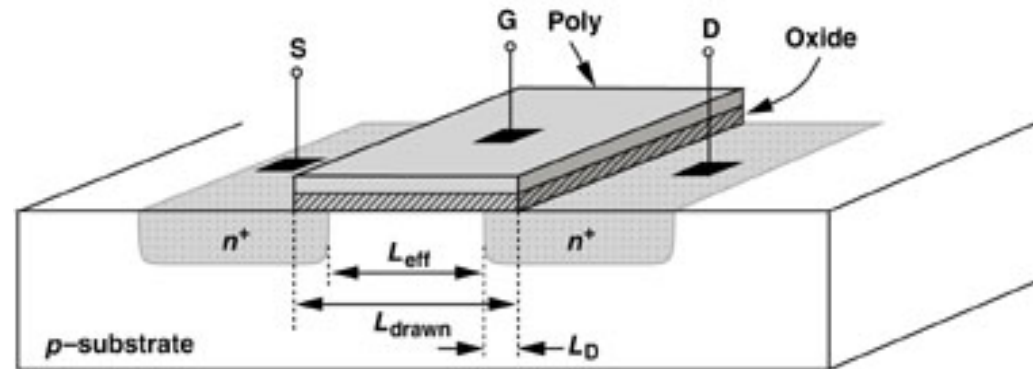


- **P-type substrate (“Bulk”, “Body”)**
- **D and S heavily doped (n^+) n-regions**
- **Gate is heavily doped polysilicon (amorphous non-crystal)**
- **Thin layer of SiO_2 to insulate Gate from Substrate**

Gate Dimensions

- **L = Length** **W = Width**
- **During fabrication S and D “side diffuse”**: Actual L is slightly less than the drawn layout L.
 - L_D = Amount of side diffusion
 - L_{Drawn} = Layout intention of L
 - L_{eff} = Effective Length
 - **Then:** $L_{\text{eff}} = L_{\text{Drawn}} - 2 L_D$

Gate Oxide thickness = t_{ox}



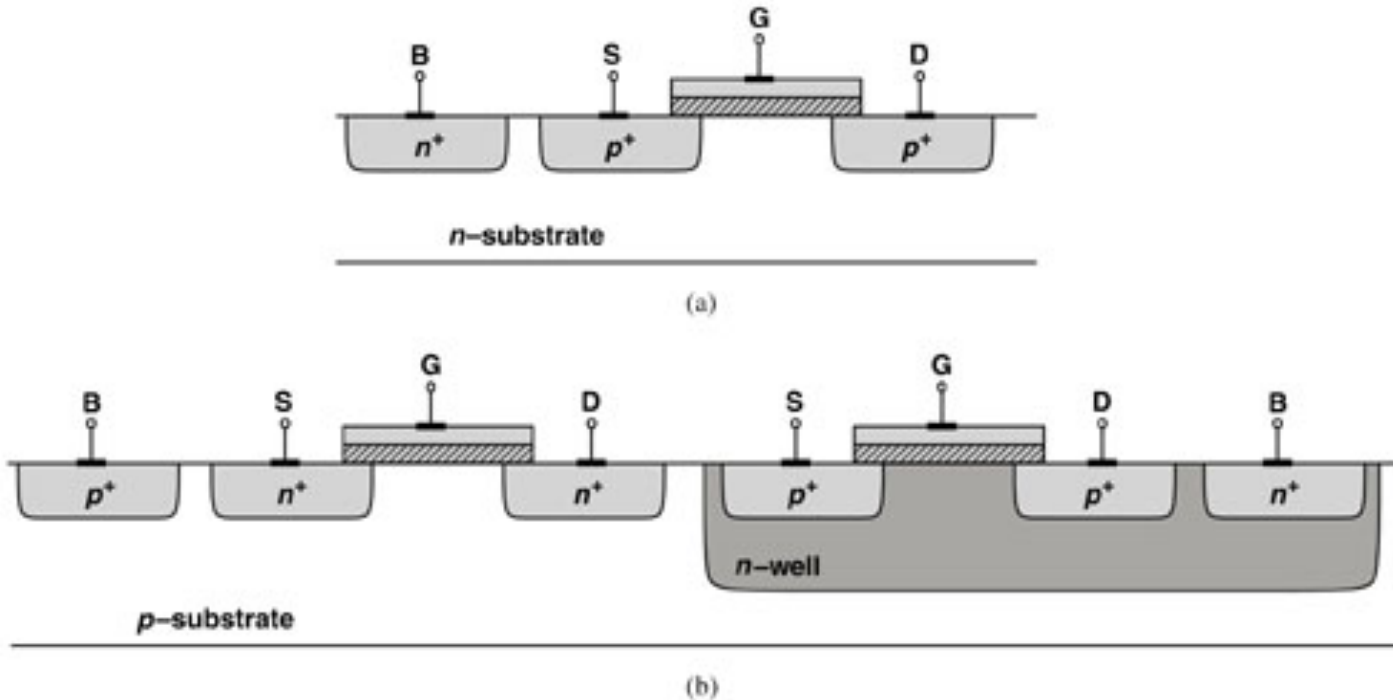
Technology Trends

- The principal thrust in MOS technology is to reduce both L and t_{ox}
- Example:

$$L_{eff} \approx 90 \text{ nm}$$

$$t_{ox} \approx 2.5 \text{ nm}$$

NMOS and PMOS with Well

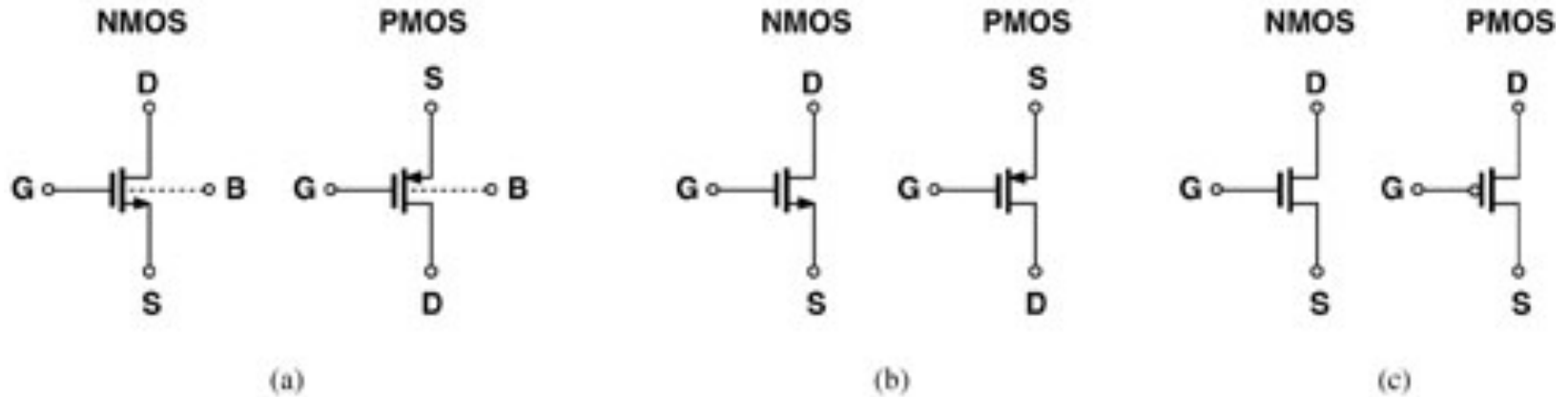


- PMOS fabricated in a “local substrate” called “well”
- All NMOS devices on a chip share the same substrate
- Each PMOS device on a chip has an independent n-well

Carriers & Currents

- **Carriers always flow from the Source to Drain**
- **NMOS: Free electrons move from Source to Drain.**
 - ❖ **Current direction is from Drain to Source.**
- **PMOS: Free holes move from Source to Drain.**
 - ❖ **Current direction is from Source to Drain.**

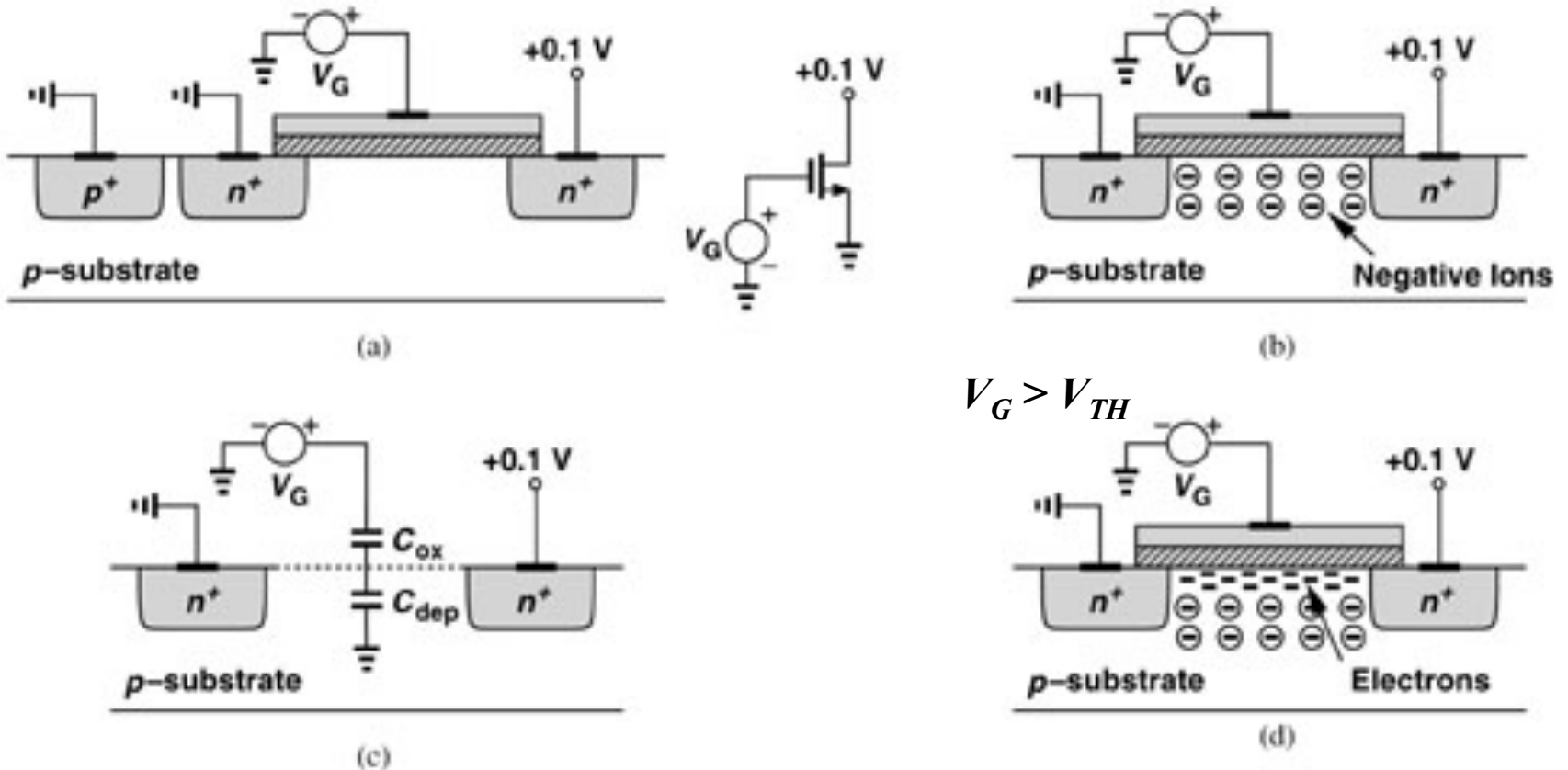
MOS Symbols



- **Symbols (a) are the most general, allowing B to be connected anywhere.**
- **Symbols (b) will be used most frequently: Whenever B of NMOS is tied to GND, or B of PMOS is tied to V_{DD}**
- **Symbols (c) used in digital circuits.**

MOS Channel Formation

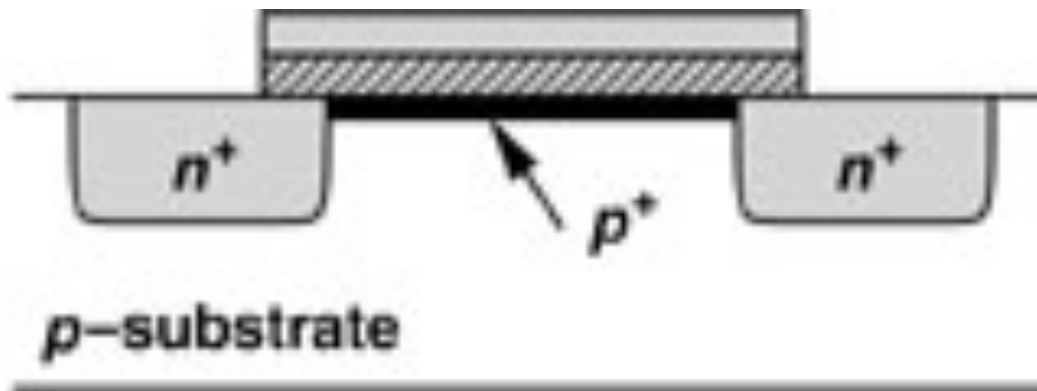
Formation of depletion region



Formation of inversion layer

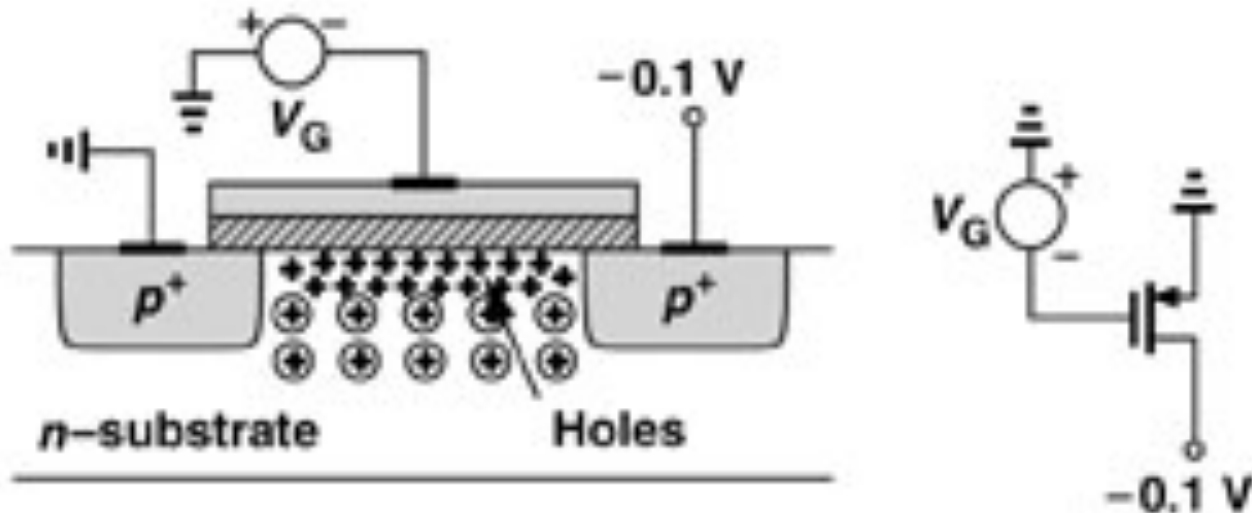
Threshold Voltage V_{TH} Adjustment

- V_{TH} is adjusted by implantation of dopants into the channel area during device fabrication.
- A thin sheet of p^+ is created, the gate voltage required to deplete this region increases.



PMOS Channel Formation

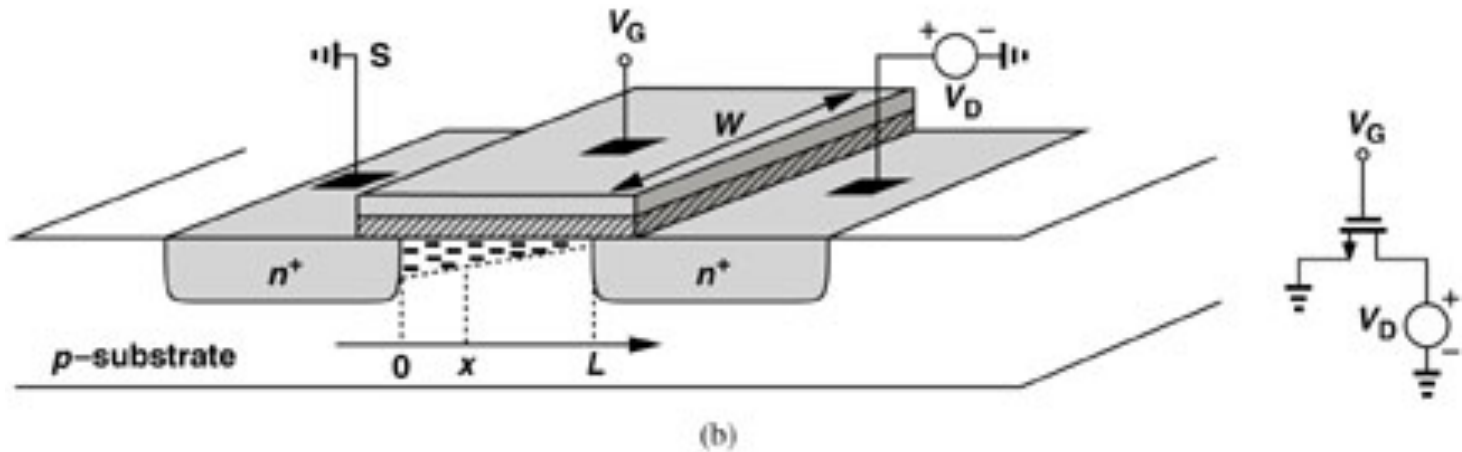
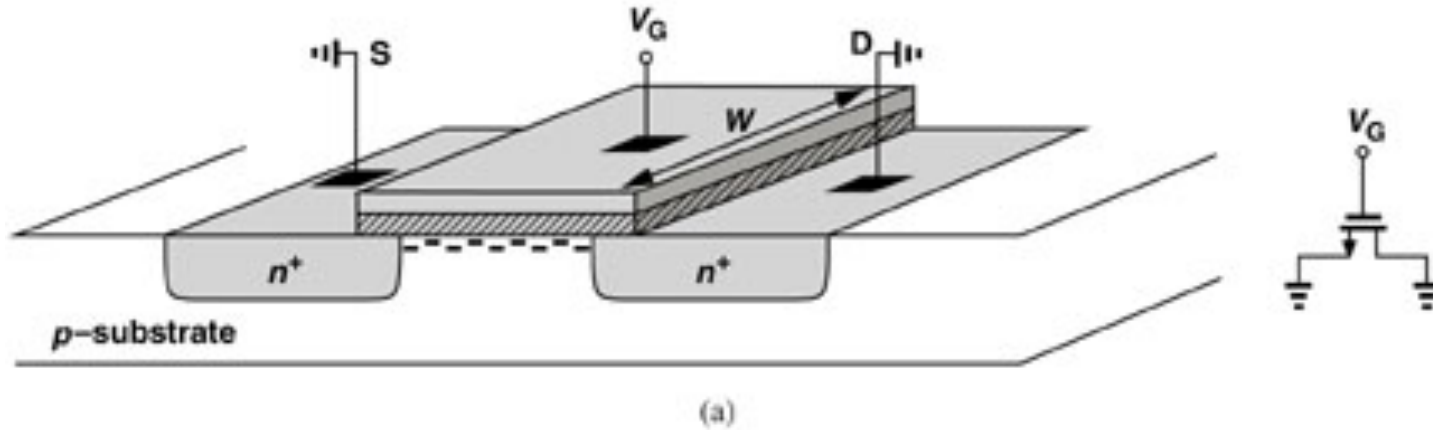
- Exactly like NMOS but with all of the polarities reversed.



- **The MOSFET structure**
- **MOS I/V Characteristics**
- **Second Order Effects**
- **MOS Device models**

I/V Characteristics

Equal source and drain voltages



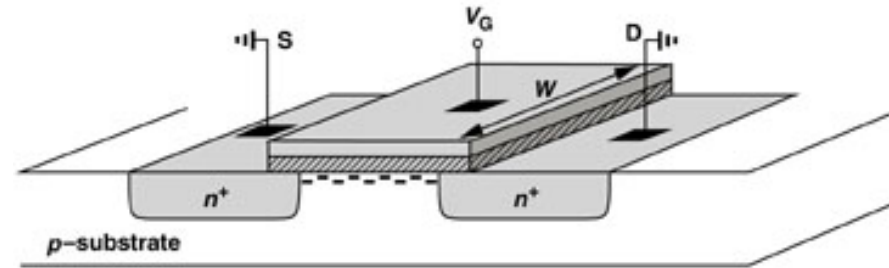
Unequal source and drain voltages

I/V Characteristics

$$I = Q_d \cdot v$$

Uniform channel charge density:

→ $Q_d = WC_{ox}(V_{GS} - V_{TH})$

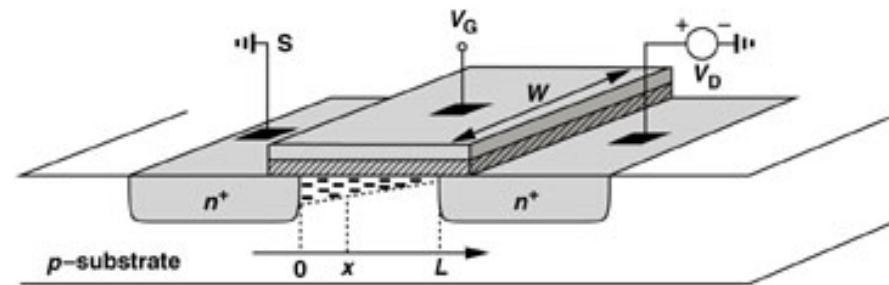


(a)

The local voltage between gate and channel varies:

→ $Q_d(x) = WC_{ox}(V_{GS} - V(x) - V_{TH})$

$$I_D = -WC_{ox}[V_{GS} - V(x) - V_{TH}] v$$



(b)

Q_d : charge density (C/m)

v : velocity of the charge (m/s)

WC_{ox} : total capacitance per unit length

I/V Characteristics (cont.)

$$I_D = -WC_{ox}[V_{GS} - V(x) - V_{TH}] v$$

$$\text{Given } v = \mu_n E \text{ and } E(x) = -\frac{dV(x)}{dx}$$

- μ_n : mobility of electrons
- E : Electric field

$$I_D = WC_{ox}[V_{GS} - V(x) - V_{TH}] \mu_n \frac{dV(x)}{dx}$$

$$\int_{x=0}^L I_D dx = \int_{V=0}^{V_{DS}} WC_{ox} \mu_n [V_{GS} - V(x) - V_{TH}] dV$$

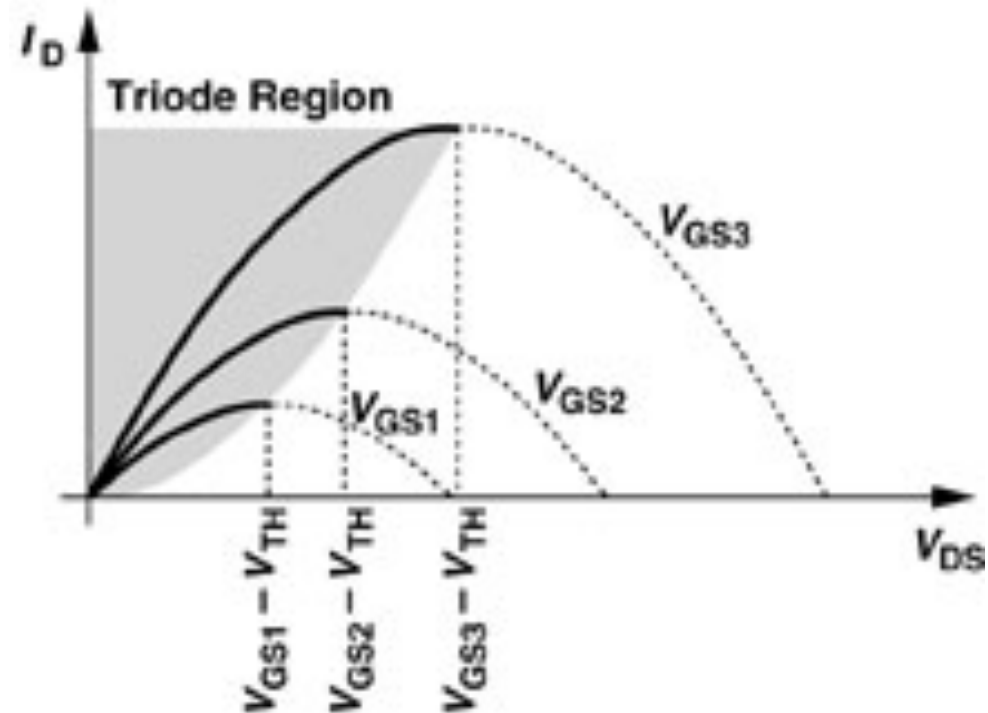
$$I_D = \mu_n C_{ox} \frac{W}{L} \left[(V_{GS} - V_{TH}) V_{DS} - \frac{1}{2} V_{DS}^2 \right]$$

I_D is constant along the channel

I/V Characteristics (cont.)

$$I_D = \mu_n C_{ox} \frac{W}{L} \left[(V_{GS} - V_{TH}) V_{DS} - \frac{1}{2} V_{DS}^2 \right]$$

$$I_{D_{\max}} = \frac{\partial I_D}{\partial V_{DS}} = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{TH})^2$$



Triode = Linear = ohmic

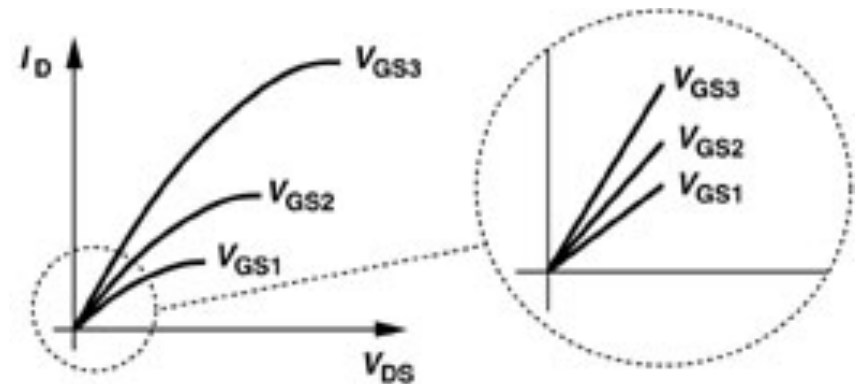
Operation in Triode Region

$$I_D = \mu_n C_{ox} \frac{W}{L} \left[(V_{GS} - V_{TH}) V_{DS} - \frac{1}{2} V_{DS}^2 \right]$$

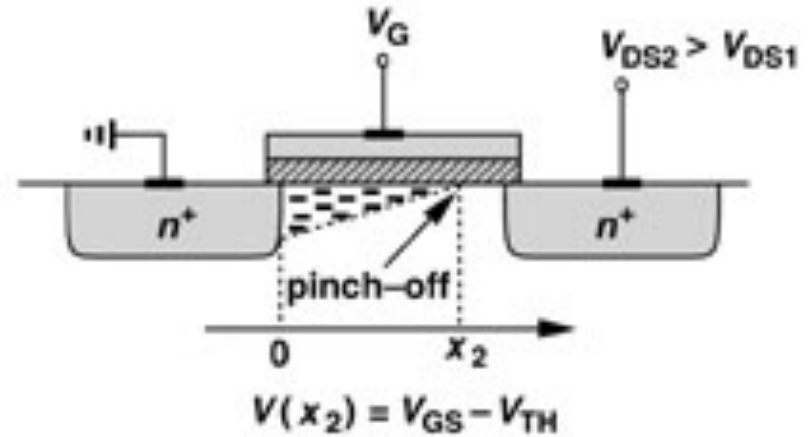
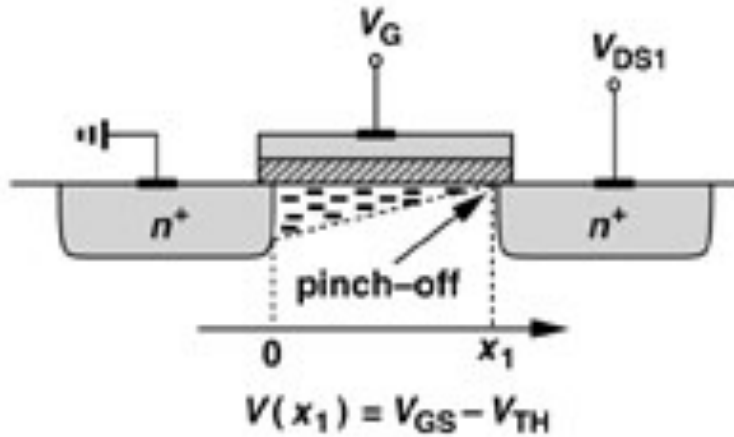
$$I_D \approx \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{TH}) V_{DS},$$

$$V_{DS} \ll 2(V_{GS} - V_{TH})$$

$$R_{ON} = \frac{1}{\mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{TH})}$$



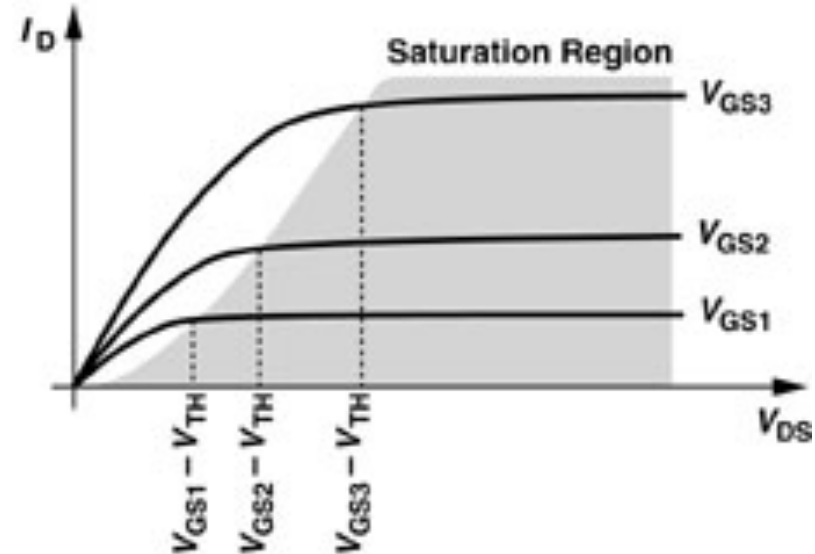
Operation in the Saturation Region



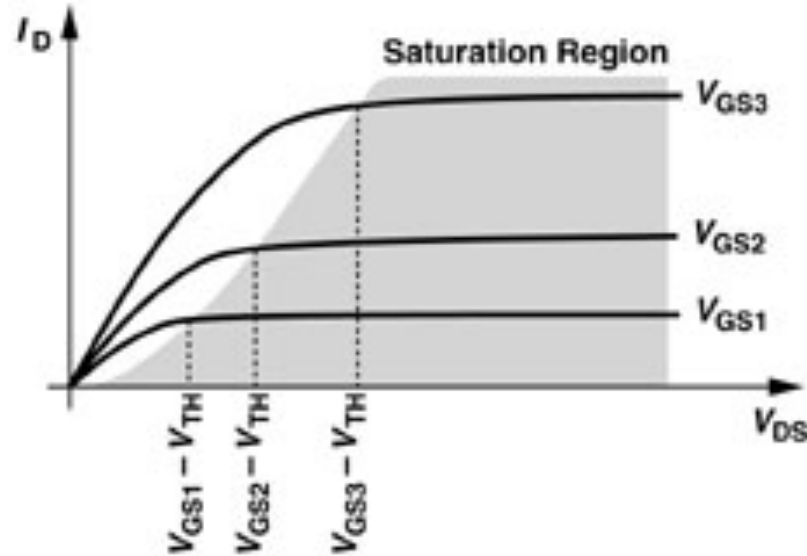
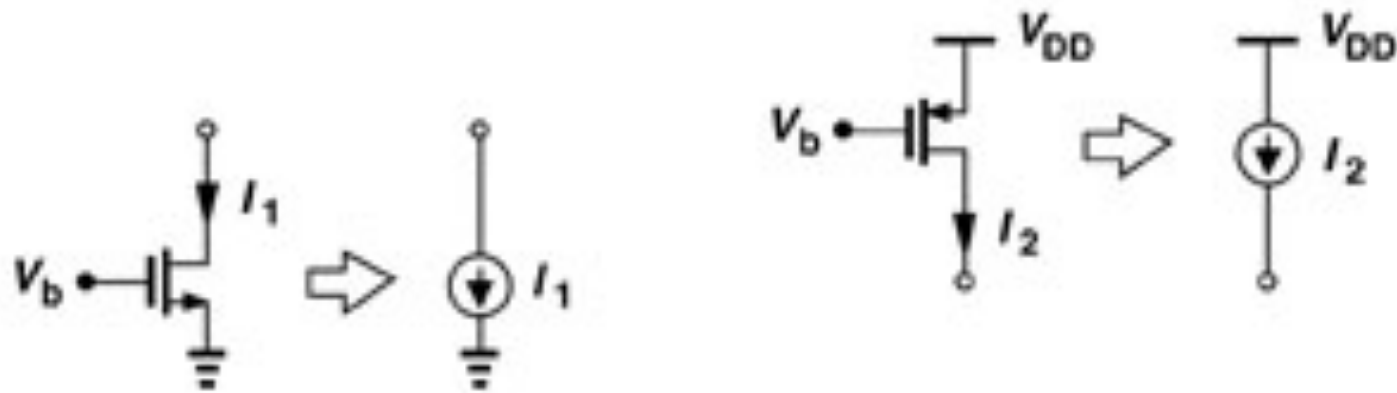
$$I_D = \mu_n C_{ox} \frac{W}{L} \left[(V_{GS} - V_{TH}) V_{DS} - \frac{1}{2} V_{DS}^2 \right]$$

$$V'_{DS} = V_{GS} - V_{TH} \quad (\text{Pinch-off})$$

$$I_D = \frac{\mu_n C_{ox} W}{2 L} (V_{GS} - V_{TH})^2$$



Saturated MOS Operating as a Current Source

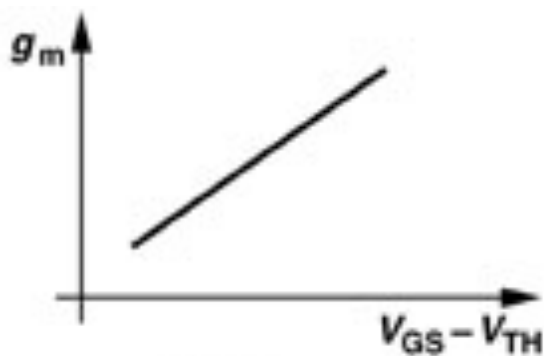


Transconductance, g_m

MOSFET operating in saturation produces a current in response to its gate-source overdrive voltage.

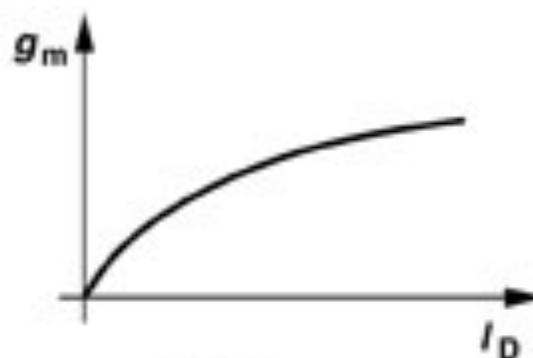
→ The transconductance is a figure of merit that indicates how well a device converts a voltage to current.

$$g_m = \left. \frac{\partial I_D}{\partial V_{GS}} \right|_{V_{DS} \text{ constant}}$$



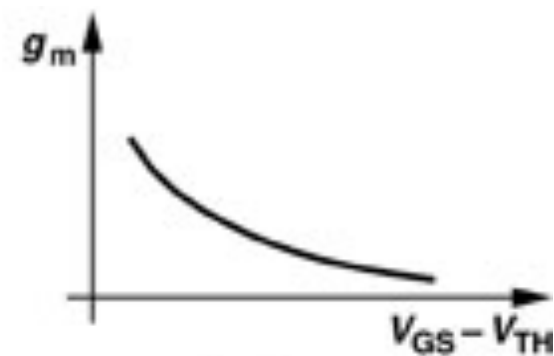
W/L Constant

$$g_m = \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{TH})$$



W/L Constant

$$g_m = \sqrt{2 \mu_n C_{ox} \frac{W}{L} I_D}$$

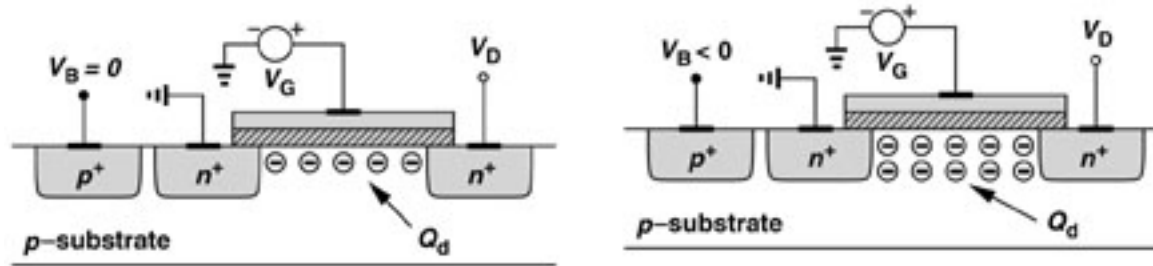


I_D Constant

$$g_m = \frac{2I_D}{V_{GS} - V_{TH}}$$

- **The MOSFET structure**
- **MOS I/V Characteristics**
- **Second Order Effects**
- **MOS Device models**

Threshold Voltage and Body Effect



$V_B \downarrow \Rightarrow$ **More holes are attracted to the substrate connection leaving a larger negative charge behind**

$$V_{TH} = V_{TH0} + \gamma \left(\sqrt{2\Phi_F + V_{SB}} - \sqrt{2\Phi_F} \right)$$

$$\gamma = \frac{\sqrt{2q\epsilon_{si}N_{sub}}}{C_{ox}}$$

$$\Phi_F = \left(\frac{kT}{q} \right) \ln \left(\frac{N_{sub}}{n_i} \right)$$

Threshold Voltage and Body Effect (cont.)

N_{sub} = doping concentration of the substrate

n_i = intrinsic carrier concentration in silicon

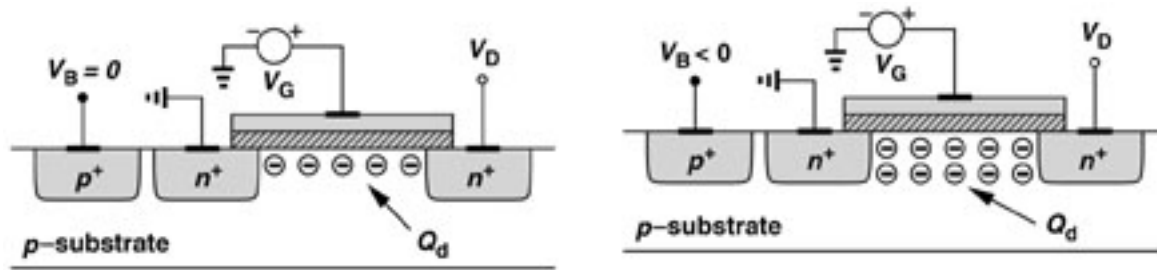
q = electron charge

Φ_F = Fermi-level

C_{ox} = gate oxide capacitance per unit area

ϵ_{si} = silicon dielectric constant

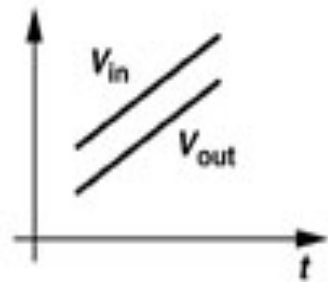
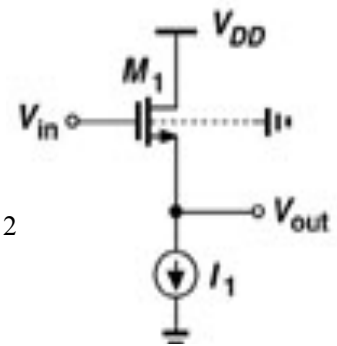
Threshold Voltage and Body Effect (cont.)



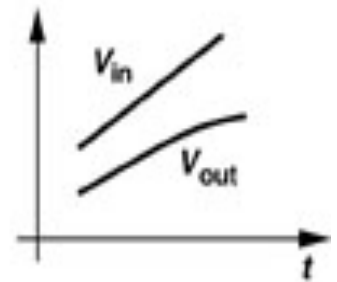
$$V_{TH} = V_{TH0} + \gamma \left(\sqrt{2\Phi_F + V_{SB}} - \sqrt{2\Phi_F} \right)$$

Example:

$$I_D = \frac{\mu_n C_{ox} W}{2 L} (V_{in} - V_{out} - V_{TH})^2$$



Without Body Effect



With Body Effect

$$V_{TH} = V_{TH0} + \gamma \left(\sqrt{2\Phi_F + V_{out}} - \sqrt{2\Phi_F} \right)$$

Bulk Transconductance, g_{mb}

$$I_D = \frac{\mu_n C_{ox}}{2} \frac{W}{L} (V_{GS} - V_{TH})^2$$

$$g_{mb} = \frac{\partial I_D}{\partial V_{BS}} = \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{TH}) \left(-\frac{\partial V_{TH}}{\partial V_{BS}} \right)$$

$$V_{TH} = V_{TH0} + \gamma \left(\sqrt{2\Phi_F + V_{SB}} - \sqrt{2\Phi_F} \right)$$

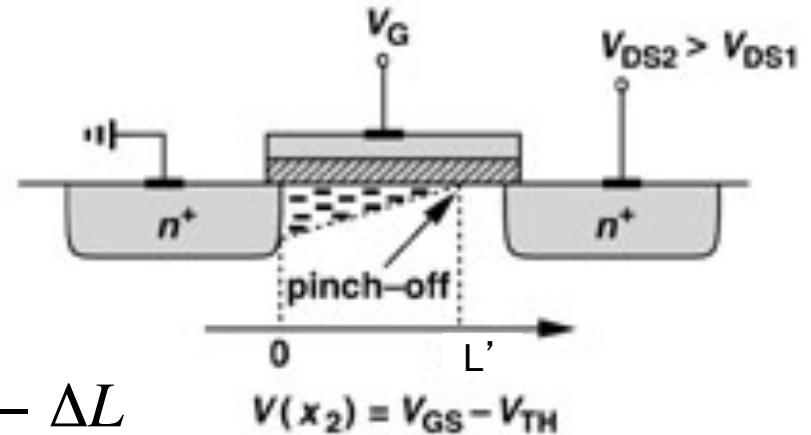
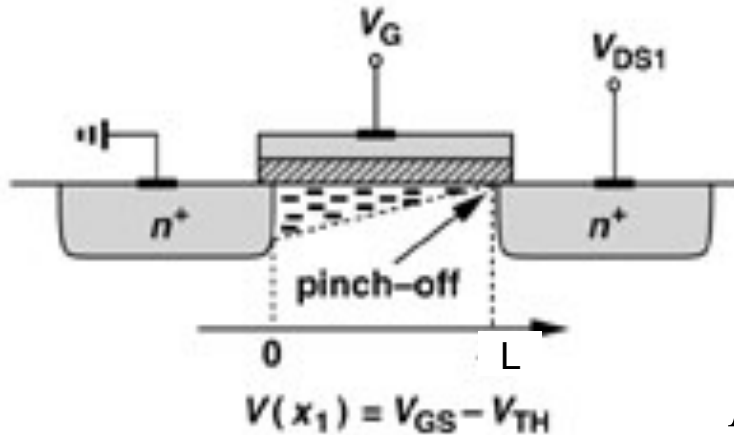
$$-\frac{\partial V_{TH}}{\partial V_{BS}} = \frac{\partial V_{TH}}{\partial V_{SB}} = \frac{\gamma}{2\sqrt{2\Phi_F + V_{SB}}} = \eta$$

$$g_{mb} = g_m \frac{\gamma}{2\sqrt{2\Phi_F + V_{SB}}}$$

$$= \eta g_m$$

$$\frac{\partial V_{TH}}{\partial V_{in}} = \eta \frac{\partial V_{out}}{\partial V_{in}}$$

Channel Length Modulation



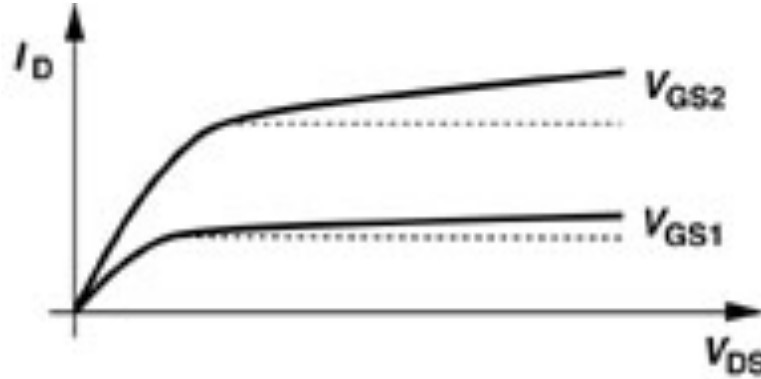
$$L' = L - \Delta L$$

$$\frac{1}{L'} \approx \frac{1}{L} \left(1 + \frac{\Delta L}{L}\right)$$

$$\frac{1}{L'} = \frac{1}{L} (1 + \lambda V_{DS}) \text{ where } \lambda V_{DS} = \Delta L / L$$

$$I_D = \frac{\mu_n C_{ox}}{2} \frac{W}{L} (V_{GS} - V_{TH})^2 (1 + \lambda V_{DS})$$

Channel Length Modulation (cont.)



$$I_D = \frac{\mu_n C_{ox}}{2} \frac{W}{L} (V_{GS} - V_{TH})^2 (1 + \lambda V_{DS})$$

$$g_m = \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{TH}) (1 + \lambda V_{DS})$$

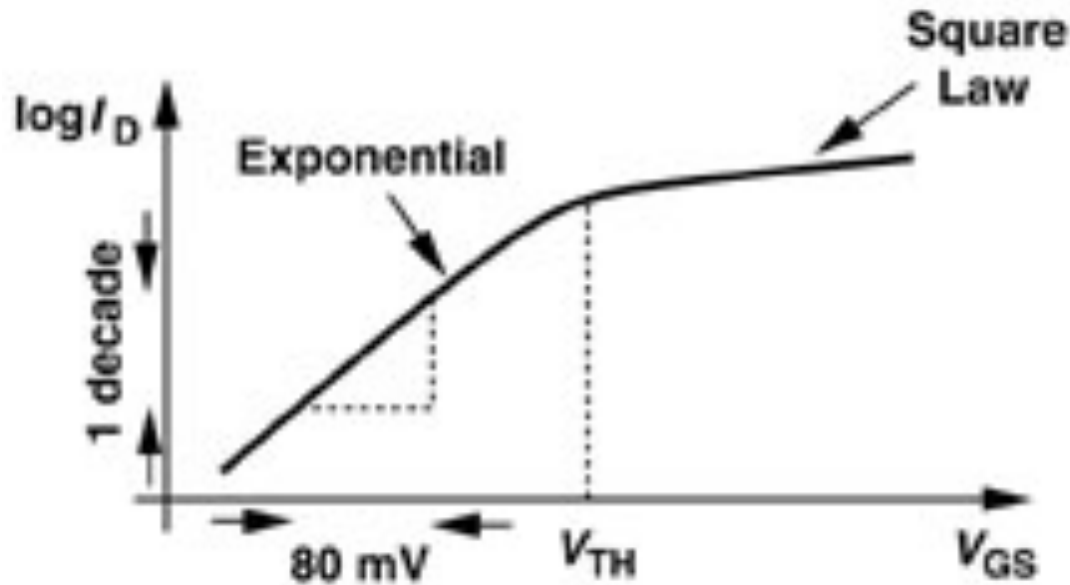
$$g_m = \sqrt{\frac{2 \mu_n C_{ox} \frac{W}{L} I_D}{(1 + \lambda V_{DS})}}$$

$$g_m = \frac{2I_D}{V_{GS} - V_{TH}}, \text{ (unchanged)}$$

Subthreshold Conduction

$$I_D = I_0 \exp\left(\frac{V_{GS}}{\xi kT/q}\right)$$

Weak Inversion



Significant current leakage for low V_{TH} !

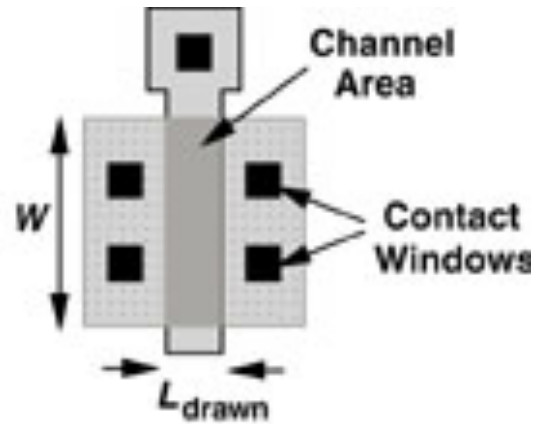
Basic MOS Device Physics

- ***The MOSFET structure***
- ***MOS I/V Characteristics***
- ***Second Order Effects***
- ***MOS Device models***

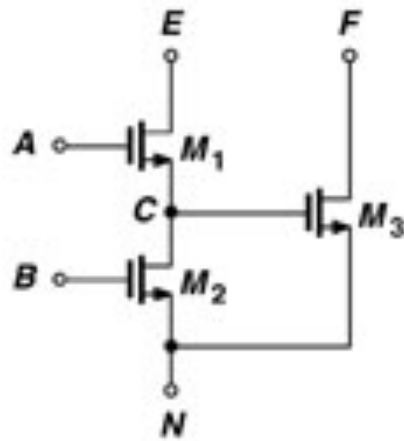
MOS Layout



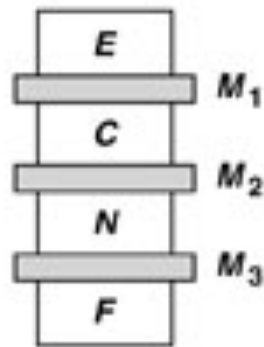
(a)



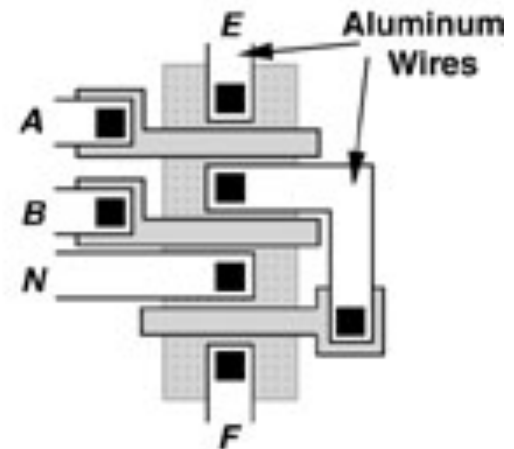
(b)



(a)

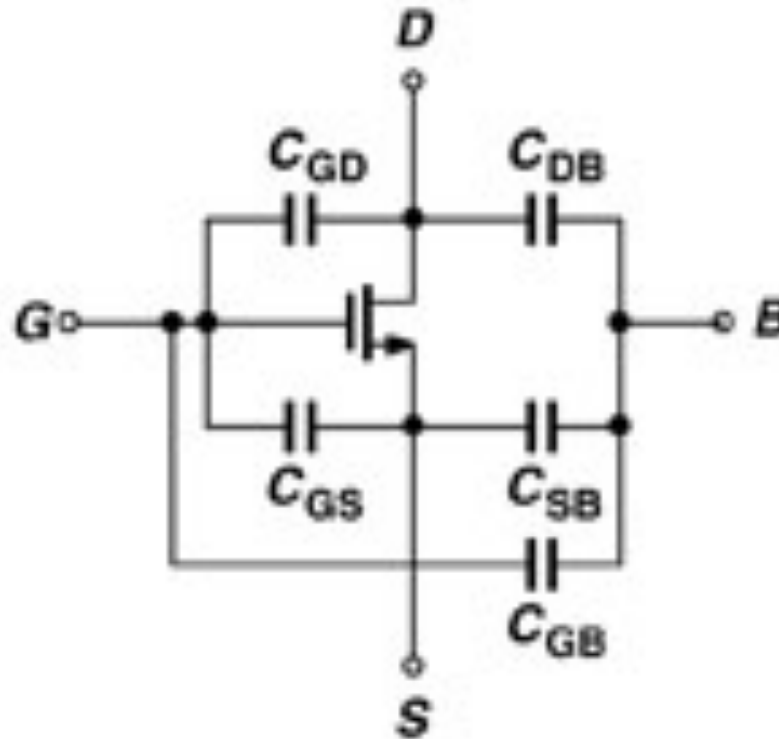


(b)

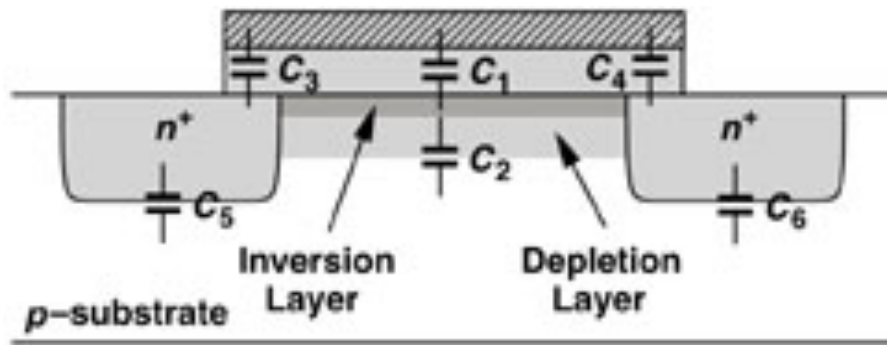


(c)

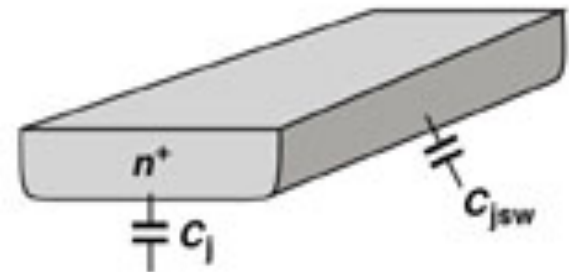
Device Capacitances



Device Capacitances



(a)



(b)

C_1 : Oxide capacitance between gate & channel

C_2 : Depletion capacitance between channel & substrate

C_3, C_4 : Overlap of the gate poly with source and drain areas

C_5, C_6 : Junction capacitance between source/drain areas and substrate

Gate-Source and Gate-Drain Capacitance

Device OFF

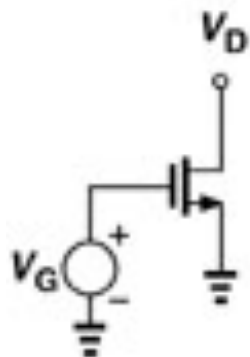
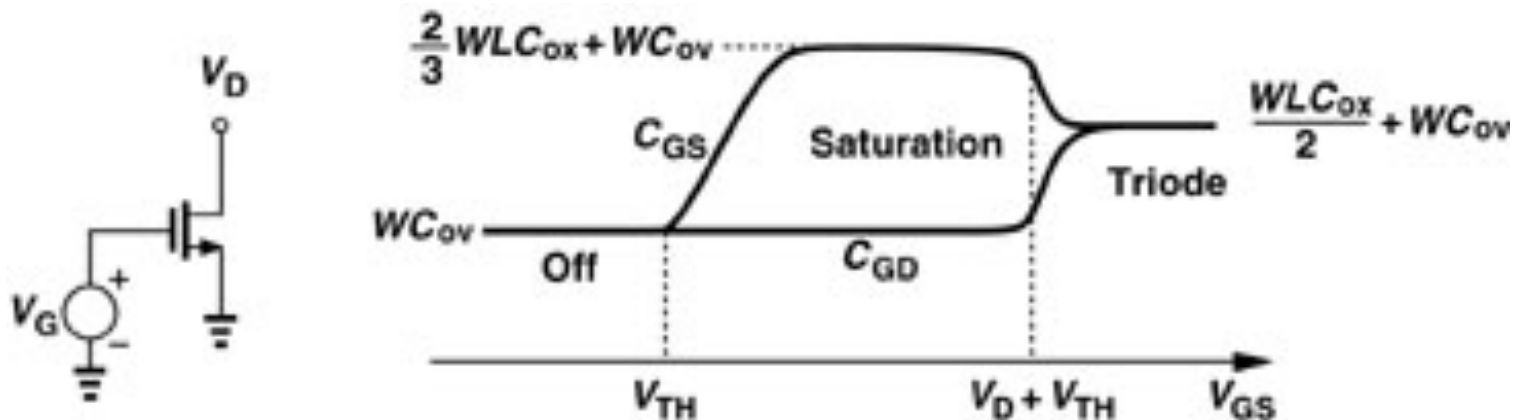
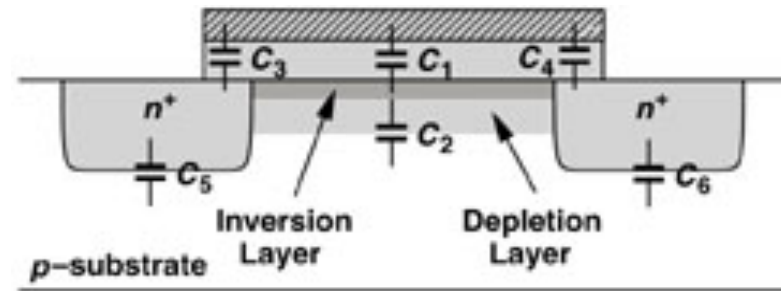
$$\rightarrow C_{GD} = C_{GS} = C_{ov}W$$

linear region $V_S \approx V_D$

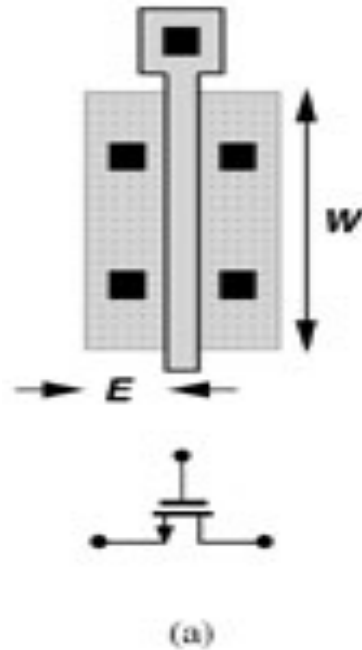
$$\rightarrow C_{GD} = C_{GS} = \frac{WLC_{ox}}{2} + C_{ov}W$$

saturation region

$$\rightarrow C_{GD} = C_{ov}W \quad \text{and} \quad C_{GS} = \frac{2}{3}WLC_{ox} + C_{ov}W$$

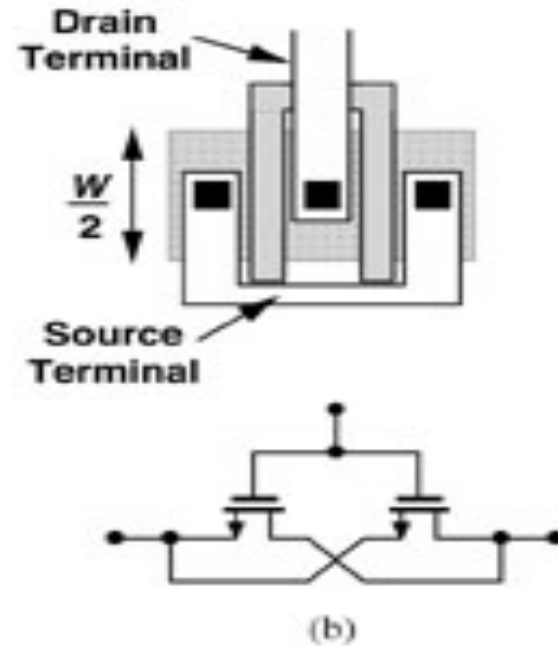


Layout for Low Capacitance



$$C_{DB} = C_{SB}$$

$$= W E C_j + 2(W + E)C_{jsw}$$

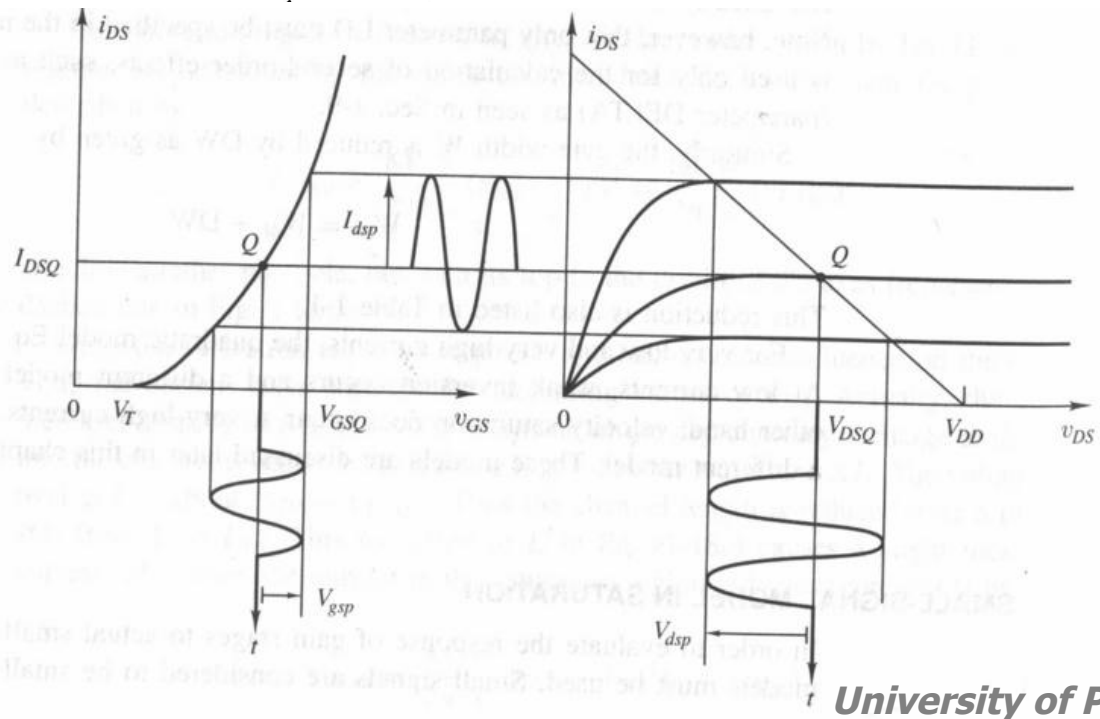
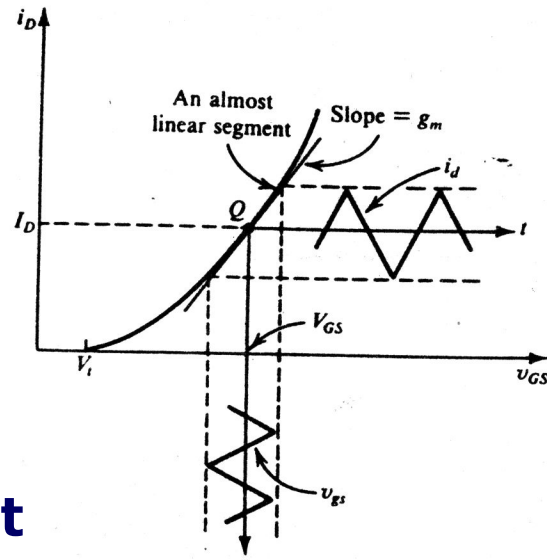


$$C_{DB} = \frac{W}{2} E C_j + 2\left(\frac{W}{2} + E\right)C_{jsw}$$

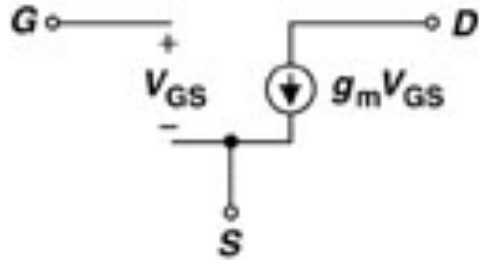
$$C_{SB} = 2 C_{DB}$$

MOS Small Signal Model

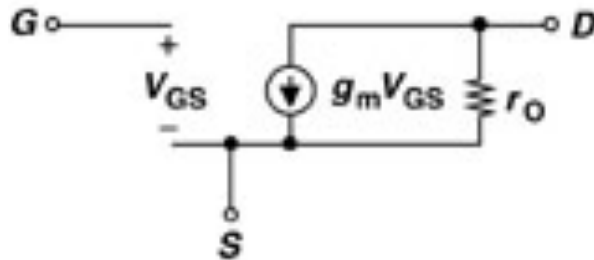
Definition:
A linear approximation
of the large signal model
around the operating point



MOS Small Signal Model



Basic MOS small signal model



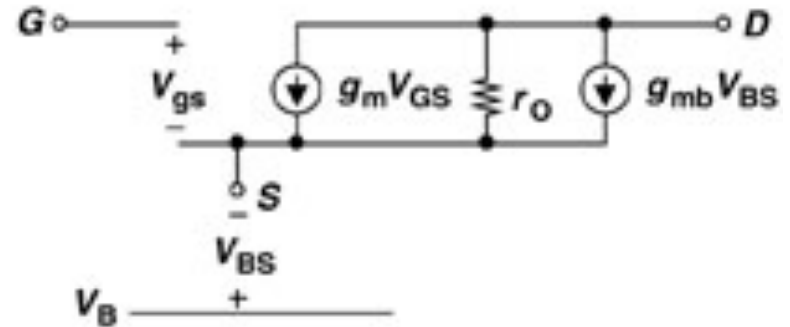
Channel length modulation represented by r_o

$$r_o = \frac{\partial V_{DS}}{\partial I_D} = \frac{1}{\partial I_D / \partial V_{DS}}$$

$$r_o = \frac{1}{\frac{\mu_n C_{ox} W}{2L} (V_{GS} - V_{TH})^2 \lambda} \approx \frac{1}{\lambda I_D}$$

MOS Small Signal Model

Body effect represented by a dependent current source

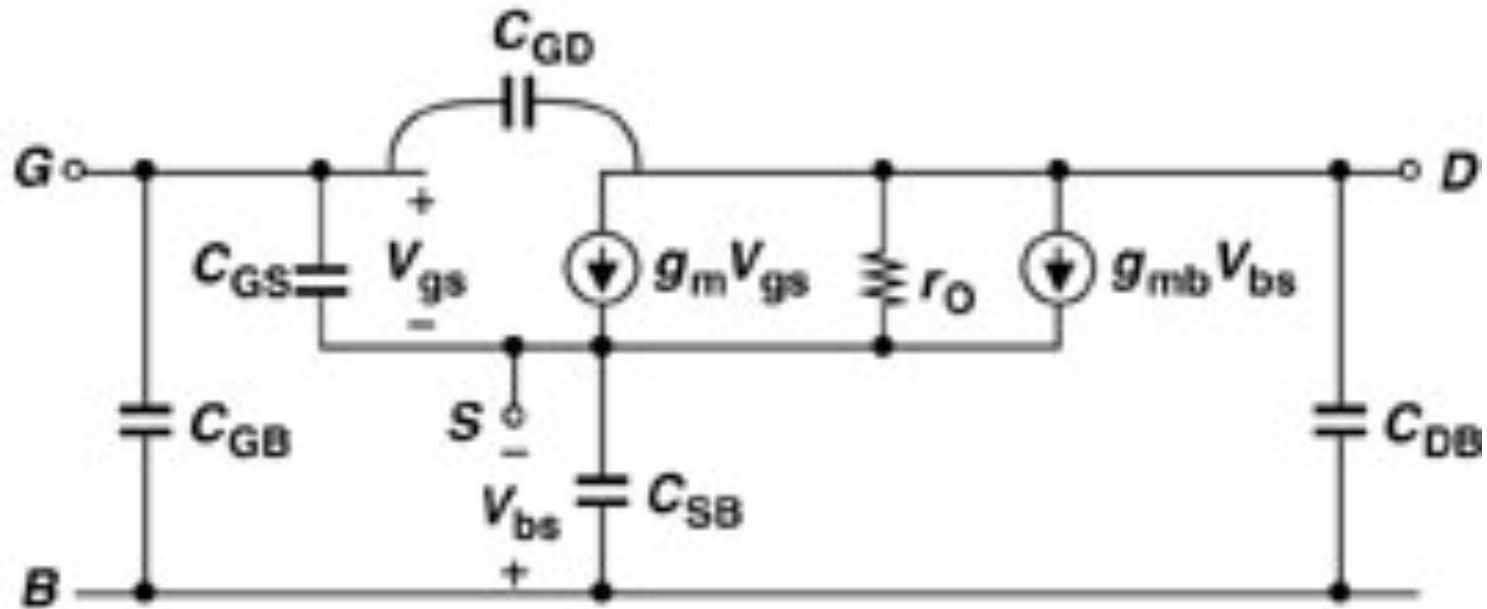


$$g_{mb} = \frac{\partial I_D}{\partial V_{BS}} = \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{TH}) \left(\frac{-\partial V_{TH}}{\partial V_{BS}} \right)$$

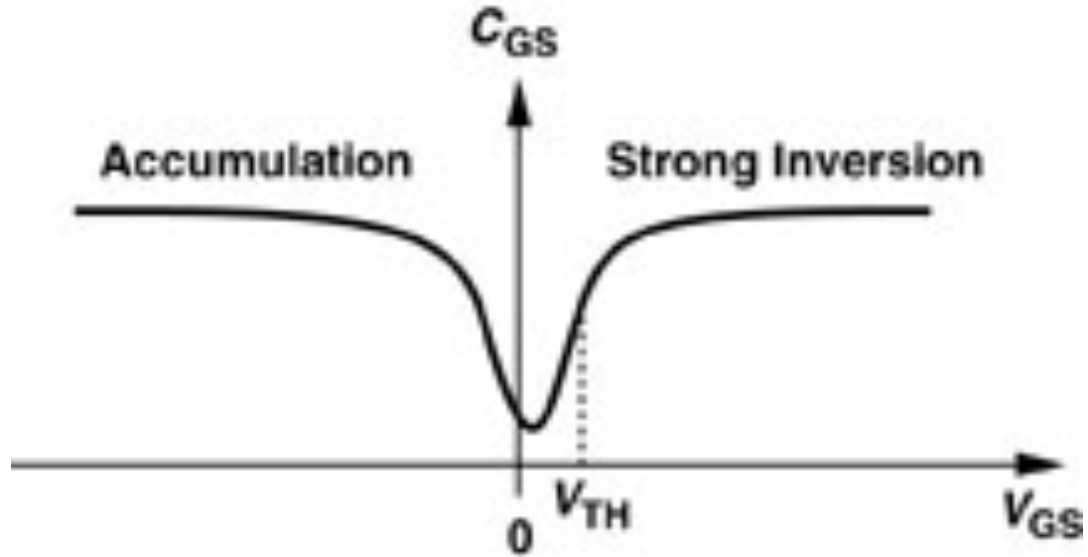
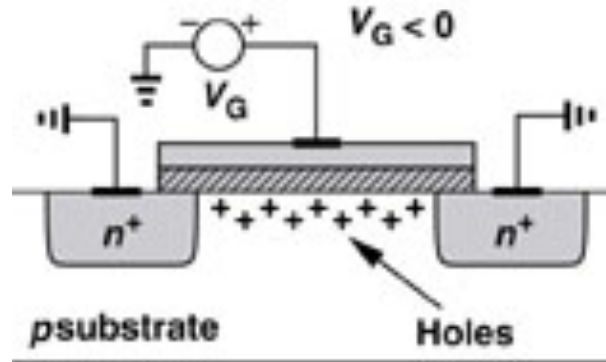
$$\frac{\partial V_{TH}}{\partial V_{BS}} = \frac{-\partial V_{TH}}{\partial V_{SB}} = -\frac{\gamma}{2} (2\Phi_F + V_{SB})^{-1/2}$$

$$g_{mb} = g_m \frac{\gamma}{2\sqrt{2\Phi_F + V_{SB}}} = \eta g_m$$

MOS Small Signal Model with Capacitance



MOS Capacitors are nonlinear



SPICE: “Simulation Program with Integrated Circuit Emphasis”

Level 1 SPICE Models for NMOS and PMOS Devices.

NMOS Model			
LEVEL = 1	VTO = 0.7	GAMMA = 0.45	PHI = 0.9
NSUB = 9e+14	LD = 0.08e-6	UO = 350	LAMBDA = 0.1
TOX = 9e-9	PB = 0.9	CJ = 0.56e-3	CJSW = 0.35e-11
MJ = 0.45	MJSW = 0.2	CGDO = 0.4e-9	JS = 1.0e-8
PMOS Model			
LEVEL = 1	VTO = -0.8	GAMMA = 0.4	PHI = 0.8
NSUB = 5e+14	LD = 0.09e-6	UO = 100	LAMBDA = 0.2
TOX = 9e-9	PB = 0.9	CJ = 0.94e-3	CJSW = 0.32e-11
MJ = 0.5	MJSW = 0.3	CGDO = 0.3e-9	JS = 0.5e-8

VTO: threshold voltage with zero V_{SB} (unit: V)

GAMMA: body effect coefficient (unit: $V^{1/2}$)

PHI: $2\Phi_F$ (unit: V)

TOX: gate oxide thickness (unit: m)

NSUB: substrate doping (unit: cm^{-3})

LD: source/drain side diffusion (unit: m)

UO: channel mobility (unit: $\text{cm}^2/\text{V}/\text{s}$)

LAMBDA: channel-length modulation coefficient (unit: V^{-1})

CJ: source/drain bottom-plate junction capacitance per unit area (unit: F/m^2)

CJSW: source/drain sidewall junction capacitance per unit length (unit: F/m)

PB: source/drain junction built-in potential (unit: V)

MJ: exponent in CJ equation (unitless)

MJSW: exponent in CJSW equation (unitless)

CGDO: gate-drain overlap capacitance per unit width (unit: F/m)

CGSO: gate-source overlap capacitance per unit width (unit: F/m)

JS: source/drain leakage current per unit area (unit: A/m^2)